

# Cryptography

## Problem set 3 - 26-27 III 2015

**Problem 1** (from the problem set no 1) Let  $\Pi_1 = \langle Gen_1, Enc_1, Dec_1 \rangle$  and  $\Pi_2 = \langle Gen_2, Enc_2, Dec_2 \rangle$  be two encryption schemes for which it is known that at least one is CPA-secure. The problem is that you don't know which one is CPA-secure and which may not be.

Show how to construct an encryption scheme  $\Pi$  that is guaranteed to be CPA-secure as long as at least one of  $\Pi_1$  or  $\Pi_2$  is CPA-secure.

Hint: Generate two plaintext messages from the original plaintext so that knowledge of either one of the parts reveals nothing about the plain-text but knowledge of both does yield the original plaintext.

Provide a full proof of your answer.

**Problem 2** Show that for a block cipher  $F'$  defined using a block cipher  $F$  by making the key longer:

$$F'_{k_1, k_2, k_3}(x) := k_1 \oplus F_{k_2}(x \oplus k_3),$$

where  $k_1, k_2, k_3$  are independent, is not secure.

**Problem 3** Consider a variant of CBC where in each encryption IV is increased by 1 (instead of choosing it at random). Show that the variant is not CPA-secure.

**Problem 4** Write a program and try to find which of the DES' S-boxes are the most linear. (The definition of the DES can be found here <http://www.itl.nist.gov/fipspubs/fip46-2.htm>).

You need to compute the probability that the following equation holds:

$$S_i(z) \oplus S_i(z \oplus x) = y,$$

for all  $i = 1, \dots, 8$ ,  $x \in \{0, 1\}^6$  i  $y \in \{0, 1\}^4$  and random  $z \in \{0, 1\}^6$ .

**Problem 5** Show that selecting S-boxes at random for an SP-network is not a good idea. Show that for randomly selected S-box linear attacks will be possible.

**Problem 6** (for Security-track, 2pts) As the problem 5 but with regard to differential attacks.